



Anonymous Crypto Currency  
**Stealth Address,  
Ring Signatures, Monero**  
Comparison to Zero.Cash



**17 B\$**



**60 M\$**

**Nicolas T. Courtois**

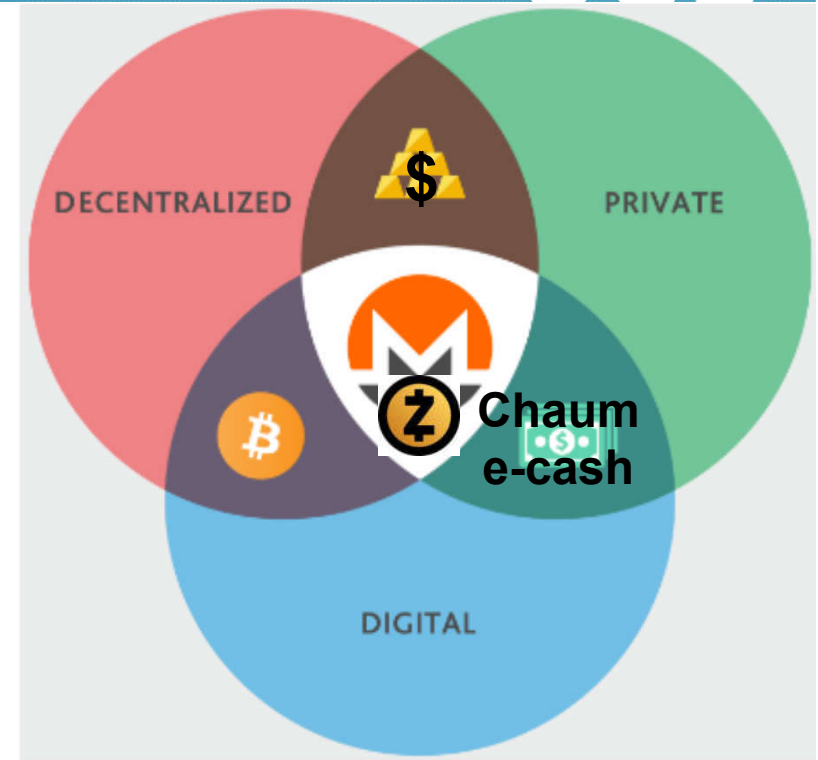
with help of Rebekah Mercer, Huanyu Ma, Mary Maller



**300 M\$**

# Topics

Bitcoin vs. Monero vs. ZCash



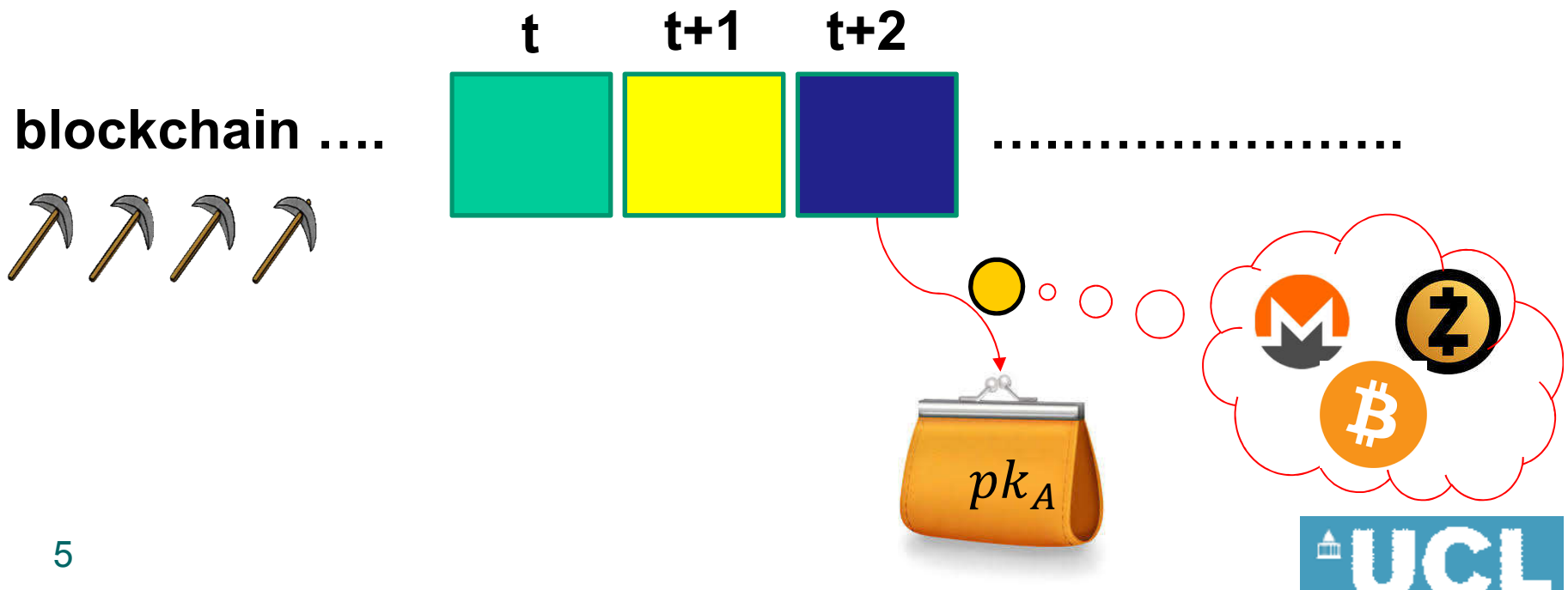
Privacy / anonymity:

- for senders [Ring Signatures,ZK proofs]
- for receivers [Stealth Address methods]
- for the transaction amount [CT] **X**

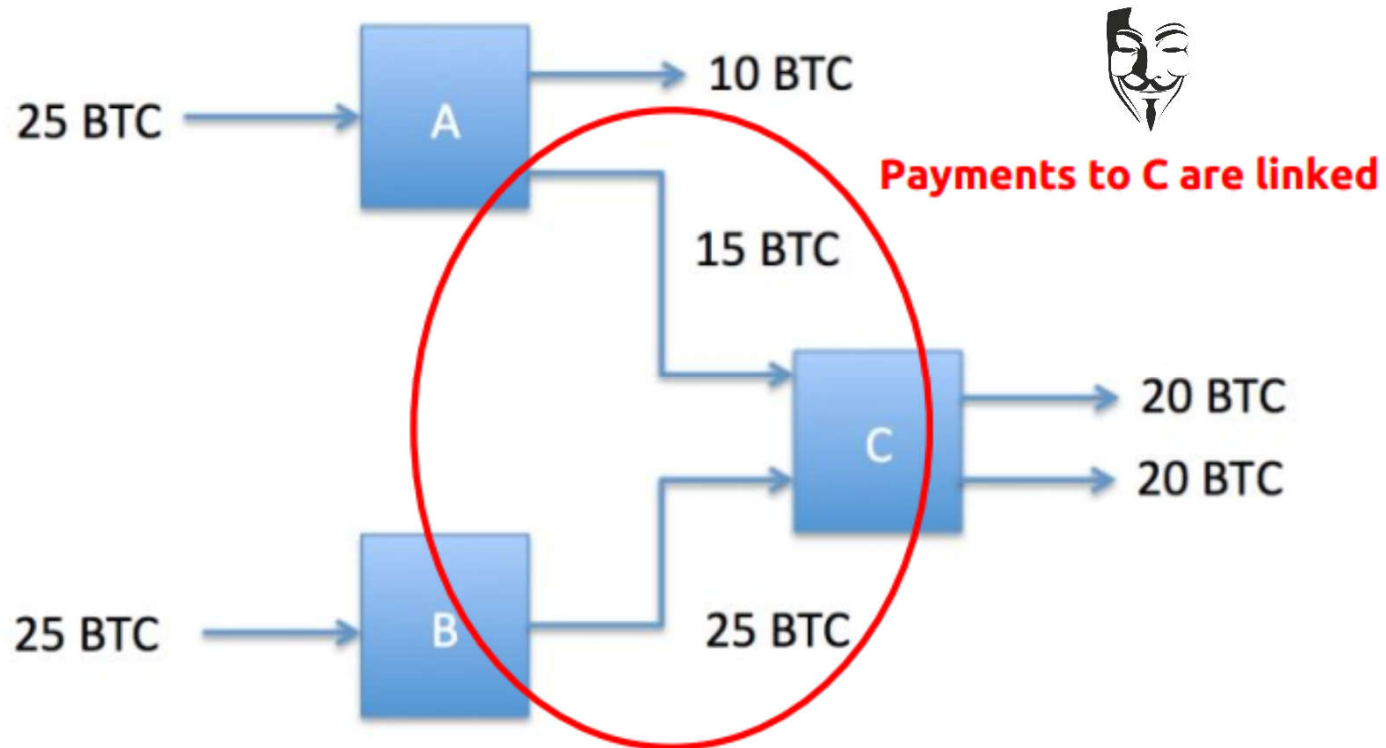
CT=Confidential Transactions,  
not studied here

# PK-based currencies

blockchain says:  
1 coin belongs to  $pk_A$

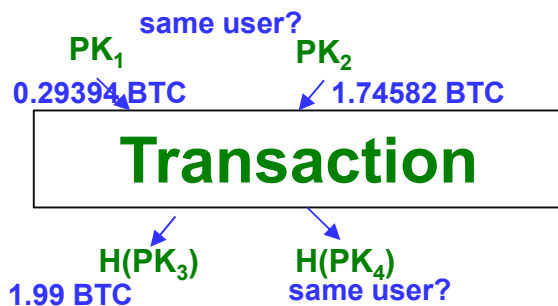
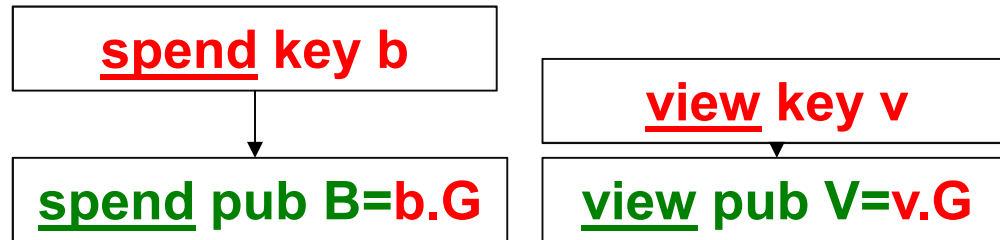
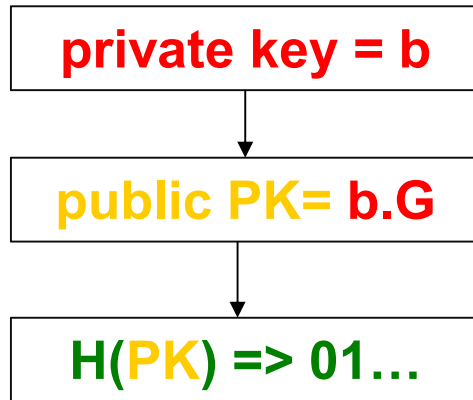


# Pb In Bitcoin



**Q: Does Monero/ZCash remove this problem????**

# \*\*Bitcoin vs. Monero



## One Time Destination key



$$H(r.V).G + B, R$$

random  $R = r.G$   
publish  $R$  with tx

Tracking key  $v, B$



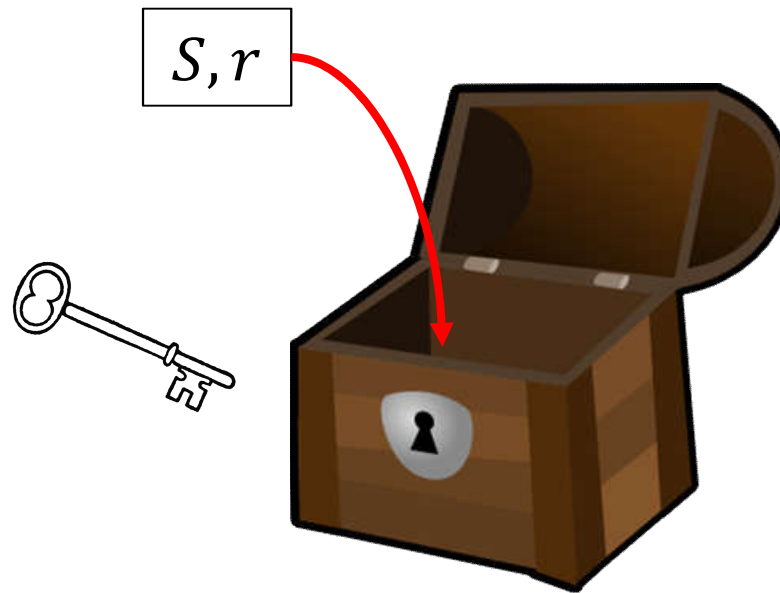
- 1000 MNR
- 100 MNR to D21...
  - 100 MNR to 2A7...
  - 100 MNR to Z93...
  - 100 MNR to P32...



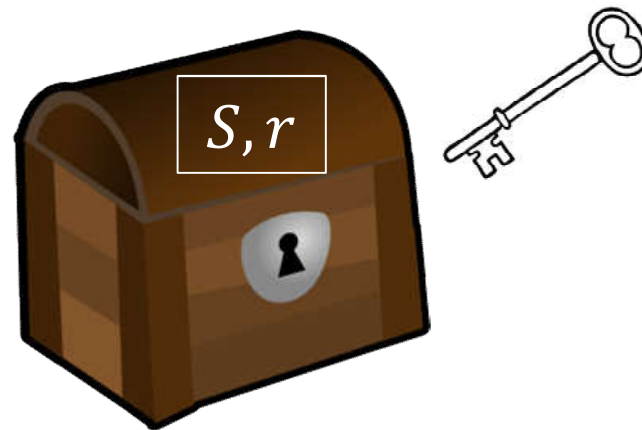
# Advanced Crypto Magic



# Commitments are used to Shield Coins:



nobody can see what is inside.



only the  
owner can  
open

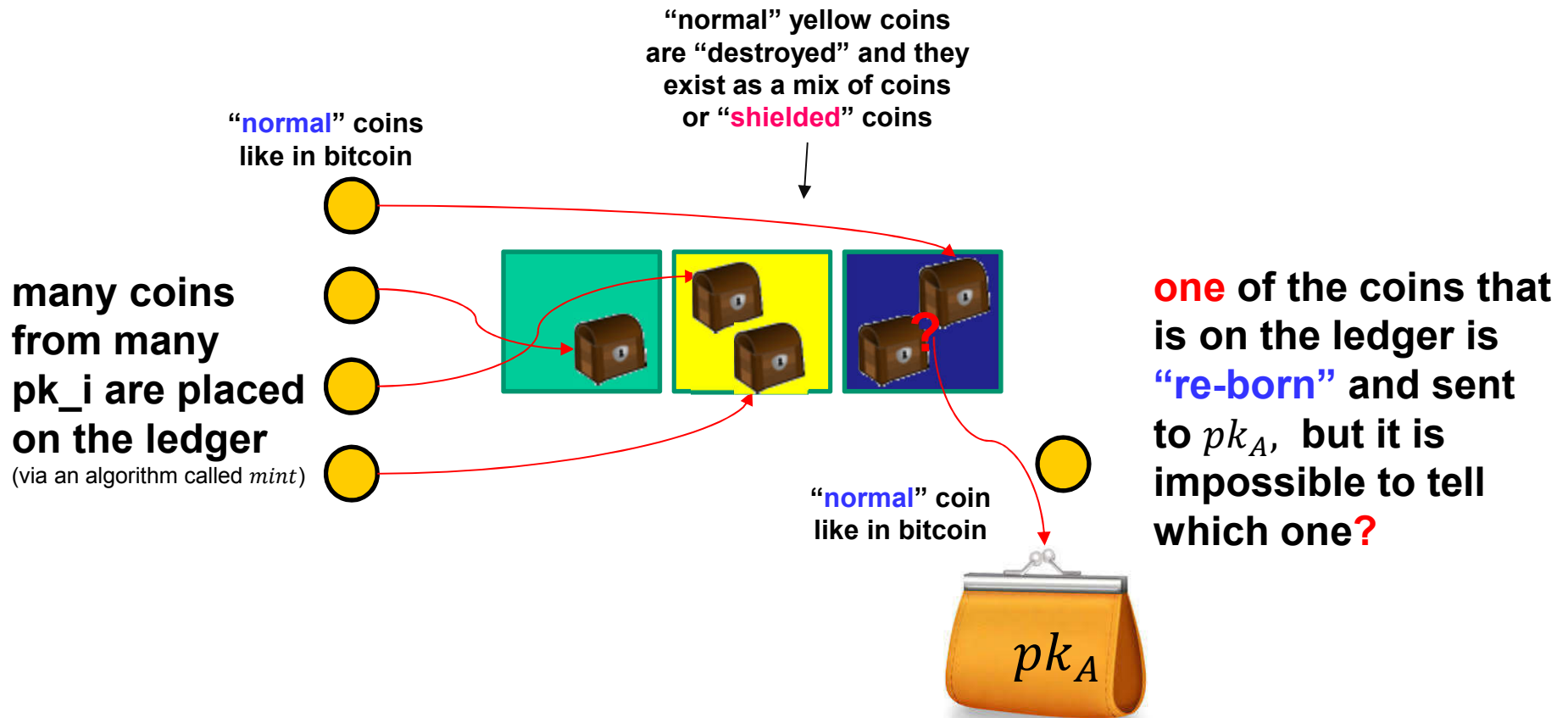
they **NEVER**  
actually get  
opened







# ZCash = a Large Scale Mixer

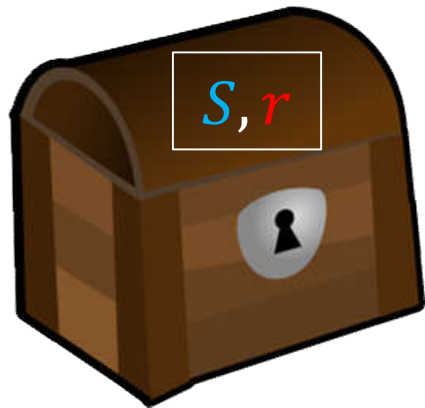


# Double Spending?

cannot be  
done twice!

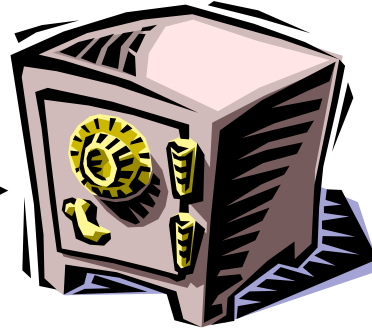
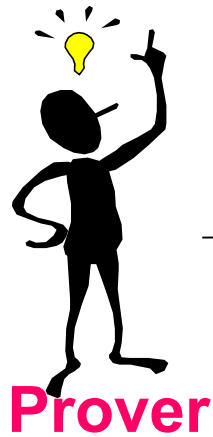
**S** is

revealed



**r** remains  
secret

# Zero-Knowledge



**Verifier**

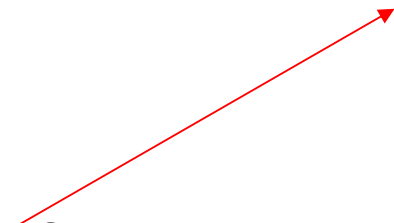
**0. Completeness** – honest signer always accepted

**1. Soundness** – dishonest signer always rejected

**2. Zero-Knowledge** – the verifier does not learn **ANYTHING**

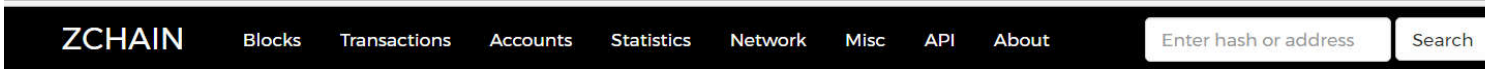


the origin of money spent



## Poor Adoption, 8GB of RAM etc...

<https://explorer.zcha.in/statistics/value>



■ Transparent (TX)
 ■ Transparent (Unspent Block Rewards)
 ■ Shielded

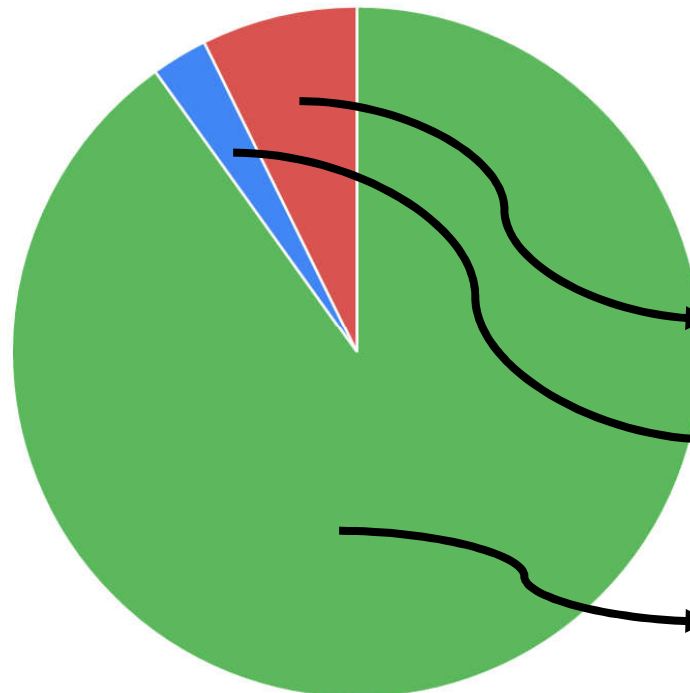


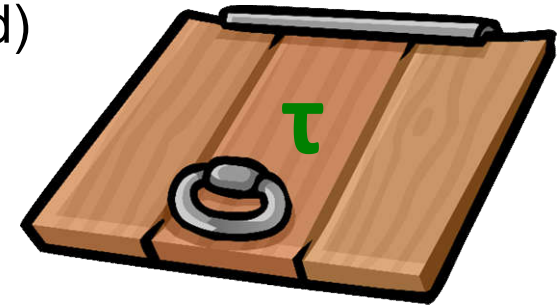
image accessed 14/03/17  
[explorer.zcha.in/statistics/value](https://explorer.zcha.in/statistics/value)

- shielded coins = 7.3%
- transparent unspent block rewards = 2.6%
- “normal” transparent coins = 90.1%



# Problems with Z.Cash

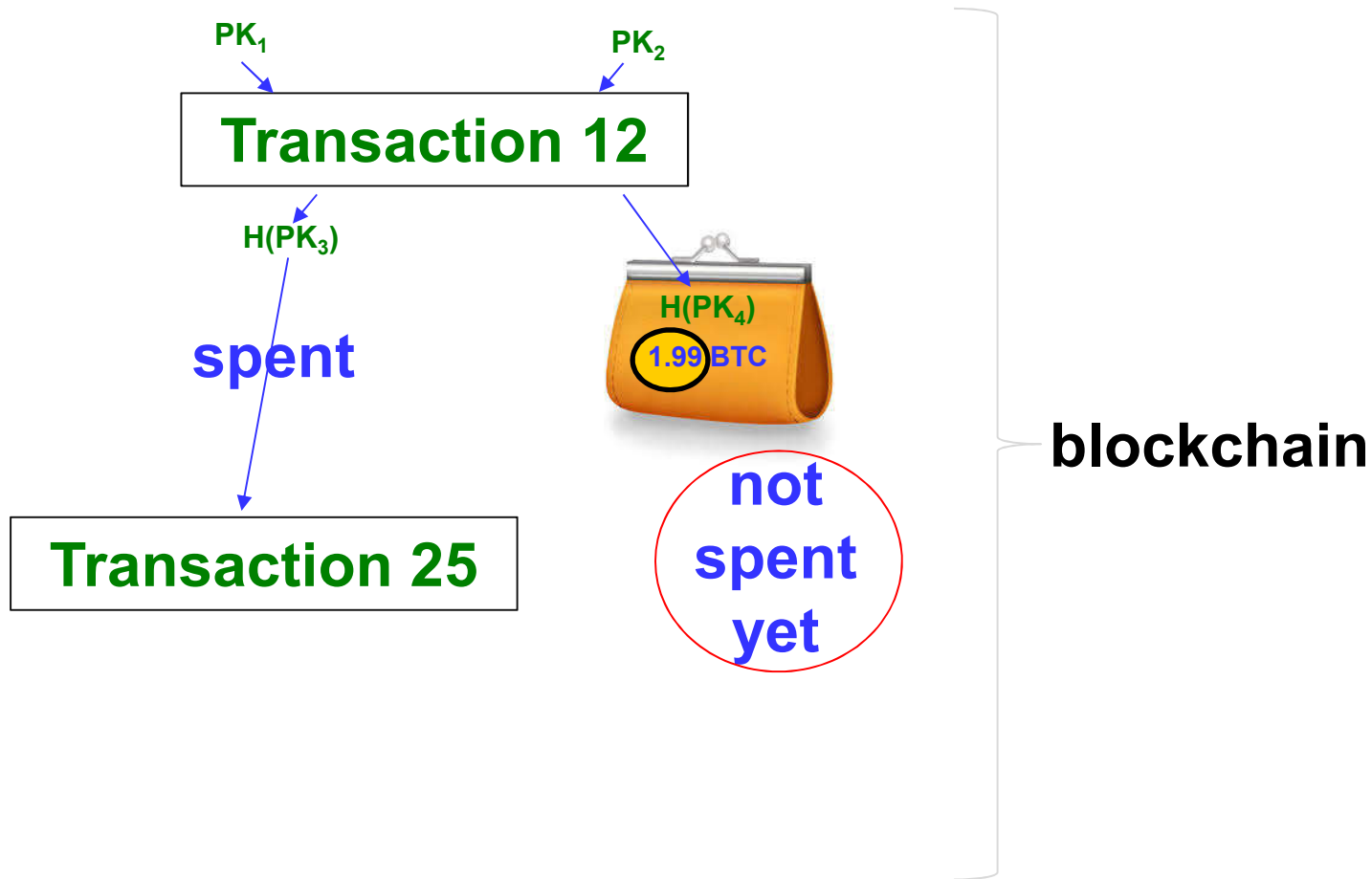
- Whoever sets-up the Z.Cash system (CRS-based) might keep hold of some **trapdoor** information.
  - This trapdoor  $\tau$  is material and real: the only hope is that it was erased!
- $\tau$  does NOT allow to steal coins of other people
- $\tau$  is NOT quantum secure:  $g^\tau \bmod p$  is published.
- But trapdoor  $\tau$  allows to create an UNLIMITED number of NEW coins!
  - current Z.Cash does not (yet) have an audit method...



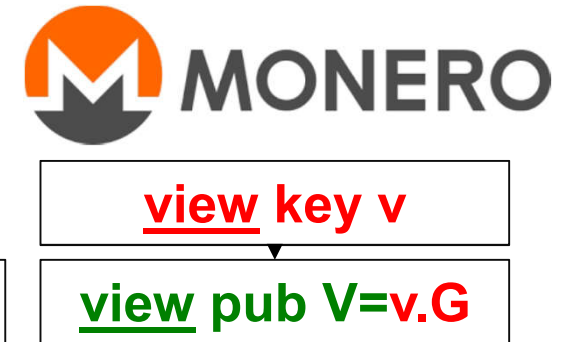
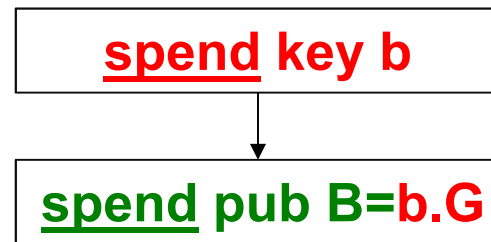
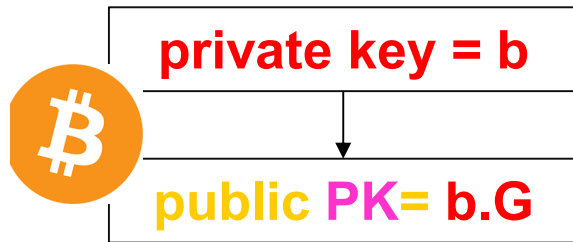
# Monero Fundamentals



def: UTXO=  
Unspent Tx Output



# Bitcoin and Monero



One Time Destination  $PK$

$$PK = H(r.V).G + B, R$$

Same Principle:

1. Money is attributed to  $PK$ ,
2. You know the ECDL of this  $PK$

=> can spend the money!

In Monero the blockchain knows NOTHING except money is flowing between 'fresh' pseudonyms  $PK$ .

(also publishes  $R$ ).





## Monero - Covert Creation of Secrets

In Monero the blockchain knows NOTHING about the receiver identity= $A, B$ , (the sender does use  $A, B$ ).

The blockchain sees only  $PK$   
and the extra number  $R$  (helps to unlock what is inside).

One Time Destination  $PK$

$$PK = H(r.V).G + B, R$$

Principle:

The receiver will have a “magical method” to compute the private key for this one-time  $PK$ .

Based on DH + extra pieces.

# Dark Wallet over Bitcoin

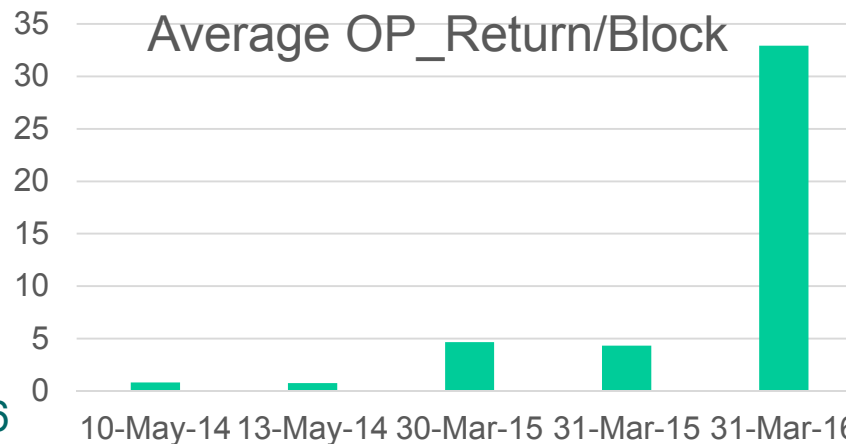
Censorship potential!

"script": "6a24aa21a9ed38538750abd25c3a84610d5b6e80c64672b01bcd3ea9d9c518f9de06288ff8d5"

Date	Avg/block
10/05/14	0.82353
13/05/14	0.75926
30/03/15	4.66667
31/03/15	4.30769
31/03/16	32.9804

One Time Destination PK

$$PK = H(r.V).G + B, R$$



# Super Dark Bitcoin

Fact:

there are methods to make these TOTALLY invisible in current bitcoin!

One Time Destination PK

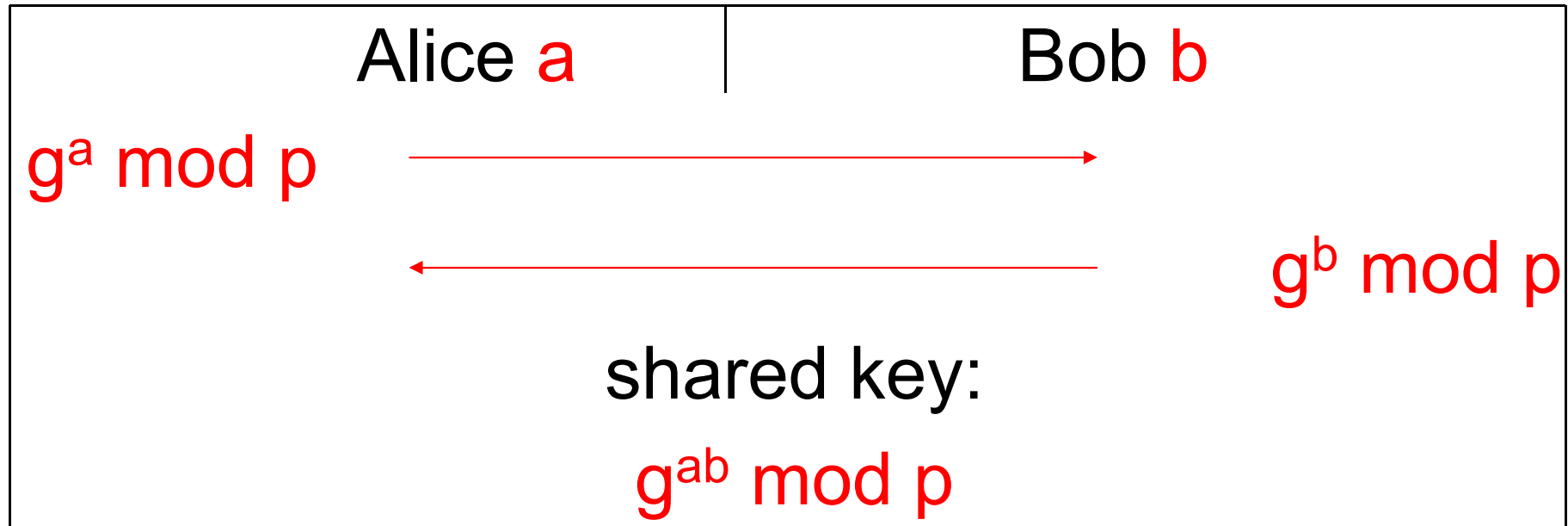
$$PK = H(a.V).G + B, A$$

Sender's PK

# Stealth Address Method[s]

(several variants)  
basic variant first

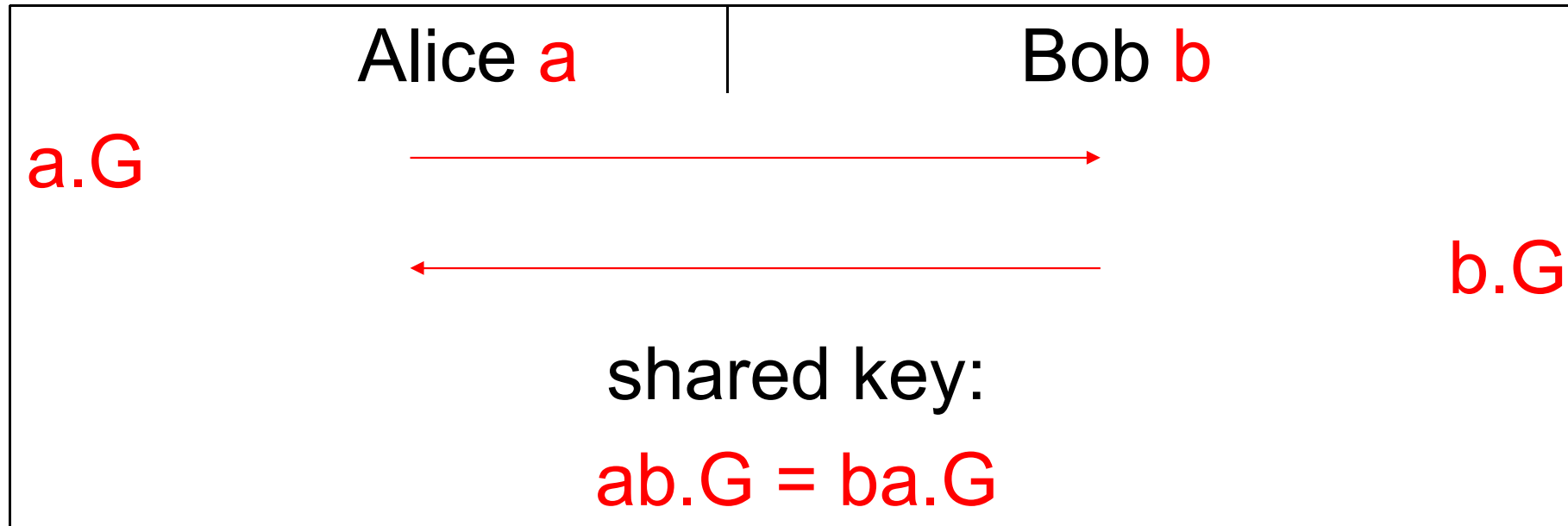
## \*Diffie-Hellman mod P



Alice computation:  $(g^b)^a = g^{ab} \bmod p$ .

Bob's computation:  $(g^a)^b = g^{ab} \bmod p$ .

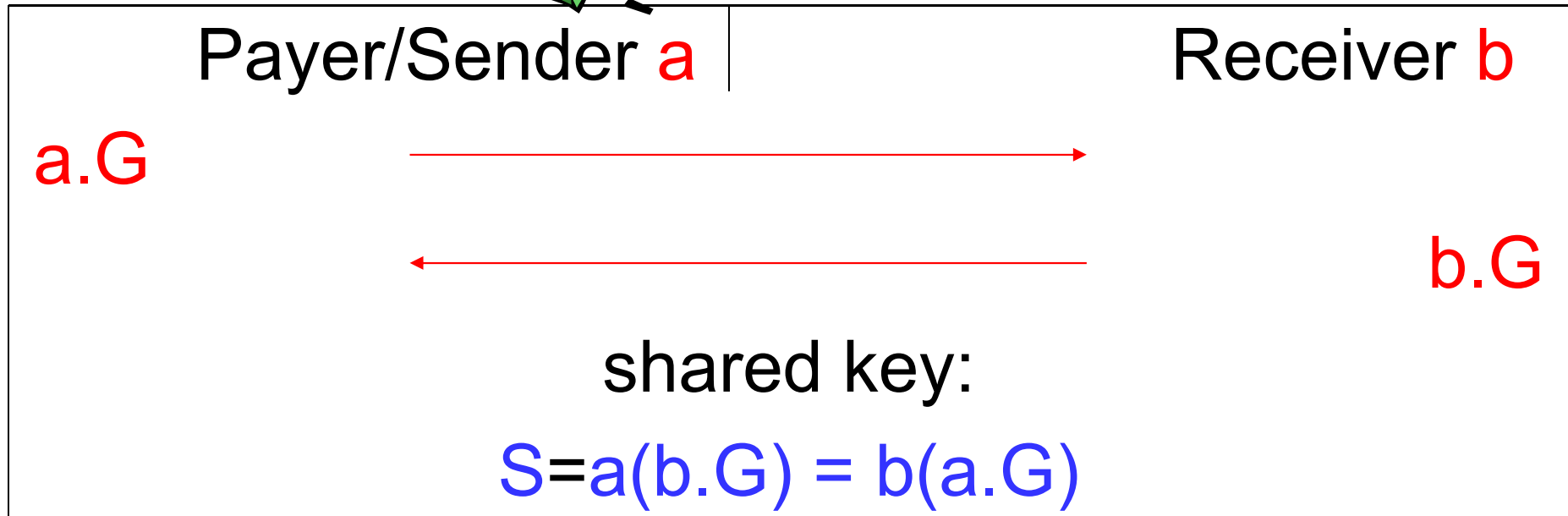
# EC Diffie-Hellman



Alice computation:  $a.(b.G)$ .

Bob's computation:  $b.(a.G)$ .

## \*\*Most Basic Stealth Address – Short Summary



Sender:  $S = a(b.G)$ . Send bitcoins to  $E = H'(H(S).G)$ .

Receiver:  $H(S) = H(b(a.G))$ . Private key  $e = H(S)$ !!!

## Stealth Address = “Invisible” Recipient

- Based on ideas by user=ByteCoin [Bitcoin forum]

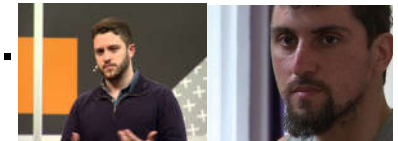
A Method to protect the recipient  
[nobody knows I sent money to this recipient]



## \*Who is using Stealth Address?

- Dark Wallet, open source BTC wallet,
  - implements 102-chars long S.A. + coin mixing.

+“permission-less!”  
-censorship pbs.

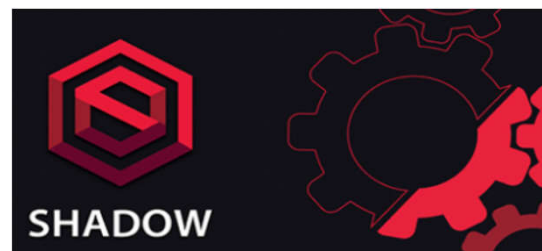


Cody Wilson Amir Taaki

- Monero
  - Market cap \$20M=>\$320M recently



- SDC = Shadow cash,
  - Market cap \$12M
- Vertcoin
  - Market Cap: \$2M



## Stealth Address = “Invisible” Recipient

- Using Diffie-Hellman. Sender= $a$  Receiver= $b$  private keys.
- Sender/A knows the recipient's public key  $b.G \bmod P$  and Rec/B knows Send/A's public key  $a.G \bmod P$ .
- Sender/A computes  $S=ab.G$ .
- A computes  $H(S)$  and generates a deterministic new bitcoin private key  $SK_{transfer}=H(S)$ . Transfer address  $E = H'(H(S).G)$ .
- A sends bitcoins to this address (Send/A could take money back!)

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- Due to DH magic, Rec/B also knows this private key  $H(b.(a.G))$ .
- B takes the money and transfers them to a new addresses,

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- Due to DH magic, Rec/B also knows this private key  $H(b.(a.G))$ .
- B takes the money and transfers them to a new addresses, quickly!!!!

# Security

- Risk:
  - The sender can spend! [Todd Jan 2014]
  - Both know **private** key **SK\_transfer**=H(S).
  - Like 24h time to think about and change his mind.
  - The receiver **MUST** be active, **ONLINE**.
    - ⇒ move money **ASAP** to another account before Sender takes it back.
    - ⇒ active/real time ⇒ easier to trace, poor anonymity,
      - good for catching criminals who ask for ransoms.

## Security (contd)

- Increased disclosure:
  - Here Recipient/B knows public key **b.G** in advance (public directory? or e.g. disclosed to any user who visits a recipient web site).
  - In bitcoin it is not disclosed  
[NSA: pls crack ECDSA/ECDL in 1 second vs. 1 year].
- Nobody knows who is the recipient of a given transaction or we cannot relate it with Recipient/B public key **b.G** even though it is in a public directory. (must keep extra data not in the blockchain).
- Deterministic: same 2 principals  $A+B \Rightarrow$  same **Transfer address E**.
- Recipient/B is **anonymous only** if he can hide his network presence (e.g. using **TOR**) when spending his attributions [issuing digital signatures].
  - He needs to be careful about how he is spending the money:  
next address not stealth, not protected!

# Improved Asymmetric Stealth Address Method

## Improved Stealth Address = Stronger Spending Key

Sender/A and Recipient/B share this common secret:

A shared bitcoin **private** key for A/B

$$H(S) = H(ab.G)$$

One can derive a **stronger**/more interesting private key like:

$$e = H(S) + b \quad \text{One Time Spending key}$$

**Asymmetry** here: Recipient/B will be the ONLY person to know **b**.

Yet Sender/A CAN compute the corresponding public key [and he knows the recipient, other people don't].

$$E = H(S).G + b.G \quad \text{One Time Destination key}$$

Later he just sends money to  $H'(E)$ .

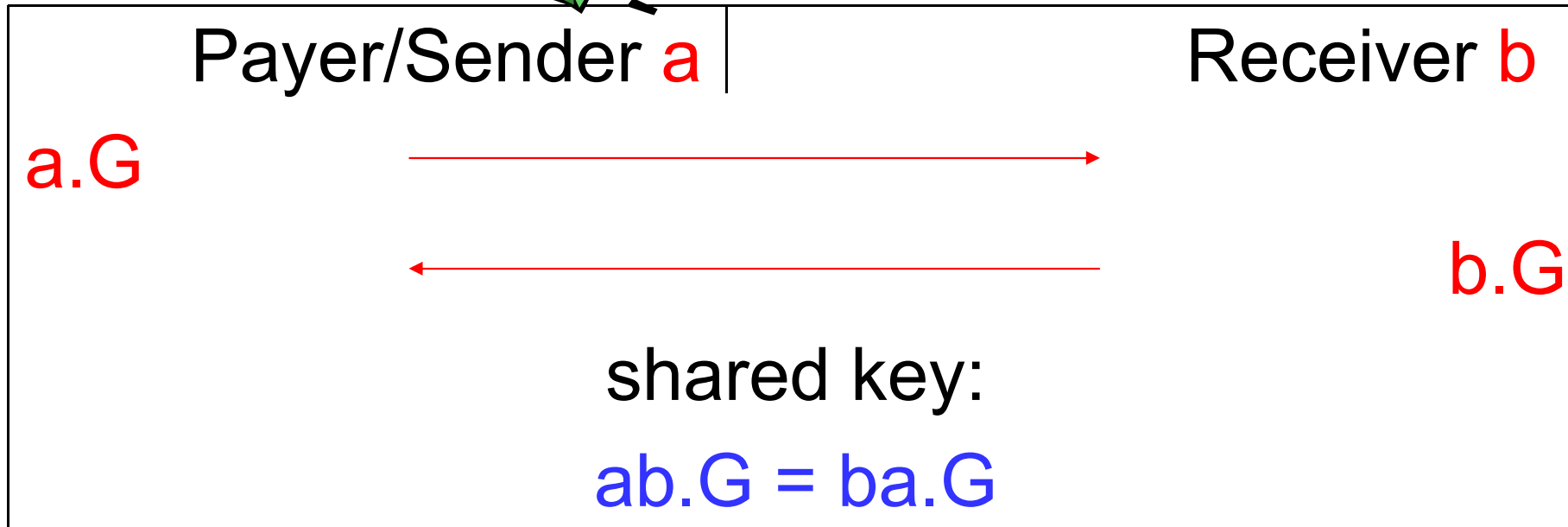
Sender cannot spend anymore!

\*inevitably E will be revealed when this money is spent further.

\*\*\*Only A and B can know if this E is valid [variant of DDH problem].



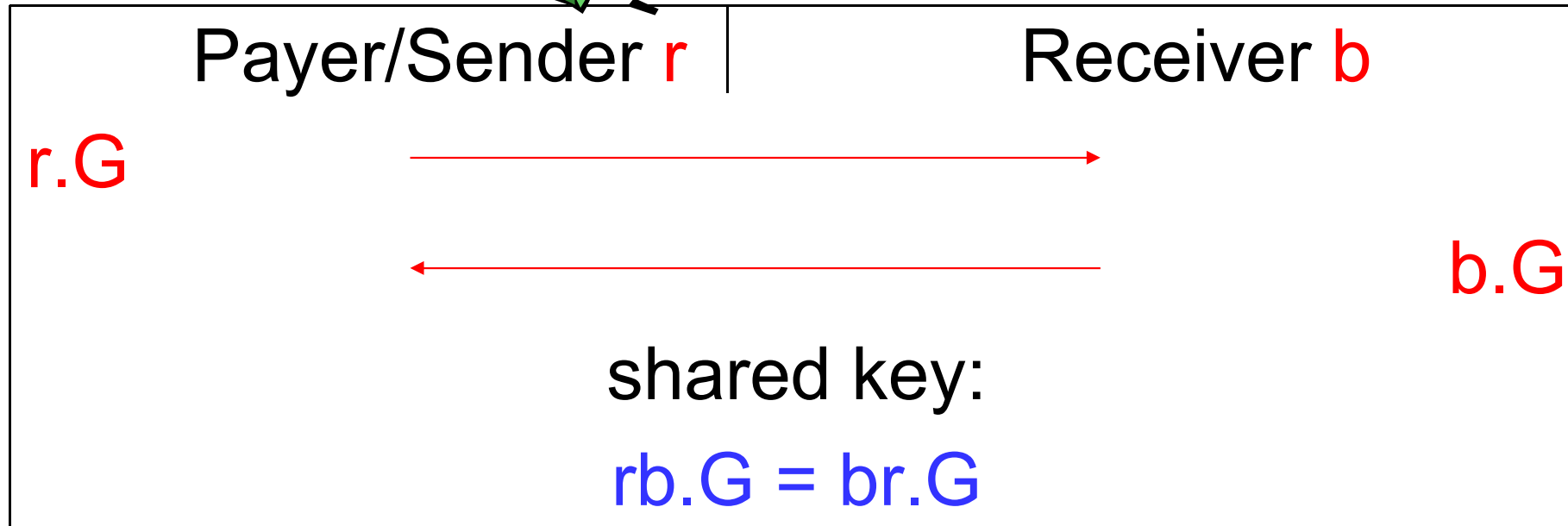
## \*Improved Stealth – DH View



Sender:  $S = a.(b.G)$ . Send bitcoins to  $E = H(S).G + b.G$ .

Receiver:  $H(S) = H(b.(a.G))$ . Private key  $e = H(S) + b!!!$

\*\*\*\* variant with **r** random nonce-keypair



Sender:  $S=r.(b.G)$ . Send bitcoins to  $E=H(S).G+b.G$ .

Receiver:  $H(S)=H(b.(r.G))$ . Private key  $e=H(S)+b!!!$

## Stealth Address - Drawbacks

- Must monitor ALL\* transactions in blockchain!!!!  
Download last few months: 1 day on a PC.

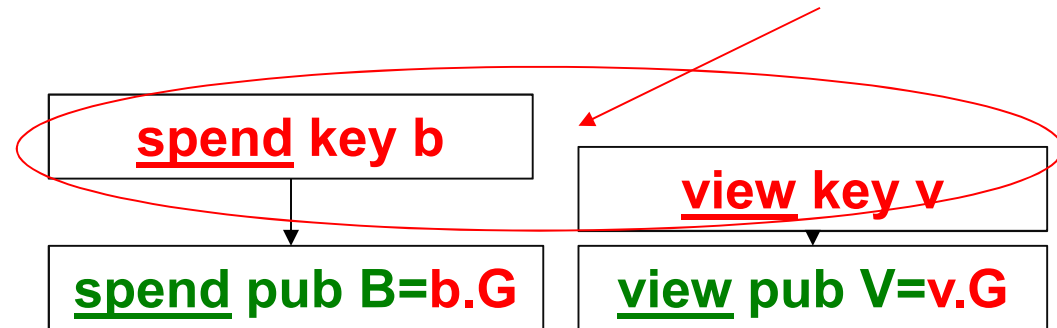
\*actually those with OP\_RETURN ==6a...

# Yet Stronger: 2xKey Stealth Address Method

## 2-Key Stealth Address

\*  $b, a$  in CryptoNote 2.0 paper  
by Nic van Sab.

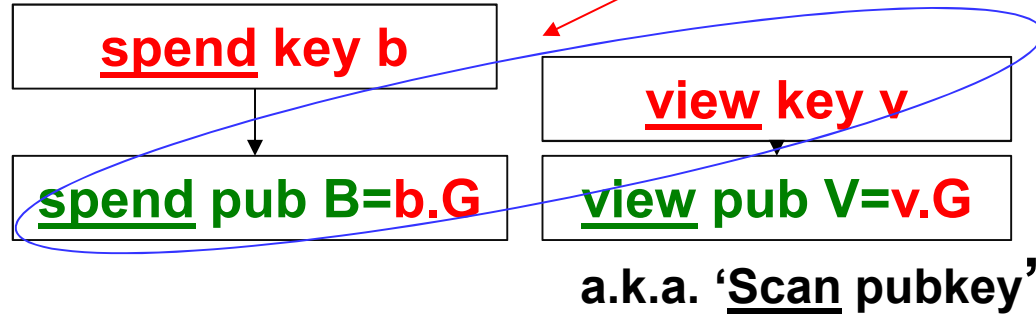
- Current private key  $b$   
will become 2 values:  
user **Private User Key** =  $b, v$
- 2 keys playing a different role,  
 $b$  is “more” secret.



# 2-Key Stealth Address

\*  $b, a$  in CryptoNote 2.0 paper by Nic van Sab.

Private User Key =  $b, v$



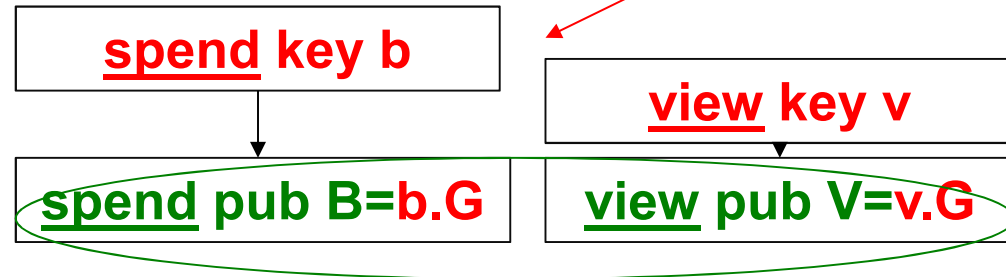
- One of them =  $v$  = View is given to a proxy entity to implement painful blockchain checks for us and notify us that payment has arrived.

Tracking Key =  $v, b.G$  (removes anonymity).

# 2-Key Stealth Address

\*  $b, a$  in CryptoNote 2.0 paper by Nic van Sab.

Private User Key =  $b, v$



Tracking Key =  $v, b.G$  (removes anonymity).

- Receiver has Public User key =  $b.G, v.G$ .

Advertised/provided/listed by the receiver, NOT visible in the blockchain transactions!

## 2-Key Stealth Address – Version A

- Recipient/B has **Private User Key** =  $b, v$
- Proxy has **Tracking Key** =  $v, b.G$  (removes anonymity).
- Receiver **Public User key** =  $b.G, v.G$ .
- Let  $S = v.(a.G) = a.(v.G)$ . Sender private  $a$ .
- Proxy and Receiver can compute  $v.(a.G)$  for every tx done by any A.
- Sender/A can do  $a.(v.G)$ .
- A sends bitcoins to  $E = b.G + H(S).G$ .
- Proxy does not know  $e$ .
- Proxy can compute  $E$  and see transactions (**view key for this tx**).
- Only the recipient has  $b$  (**spend key for this tx**).
  - Private key  $e = b + H(S)$  allows to spend the bitcoins sent to  $E$ .



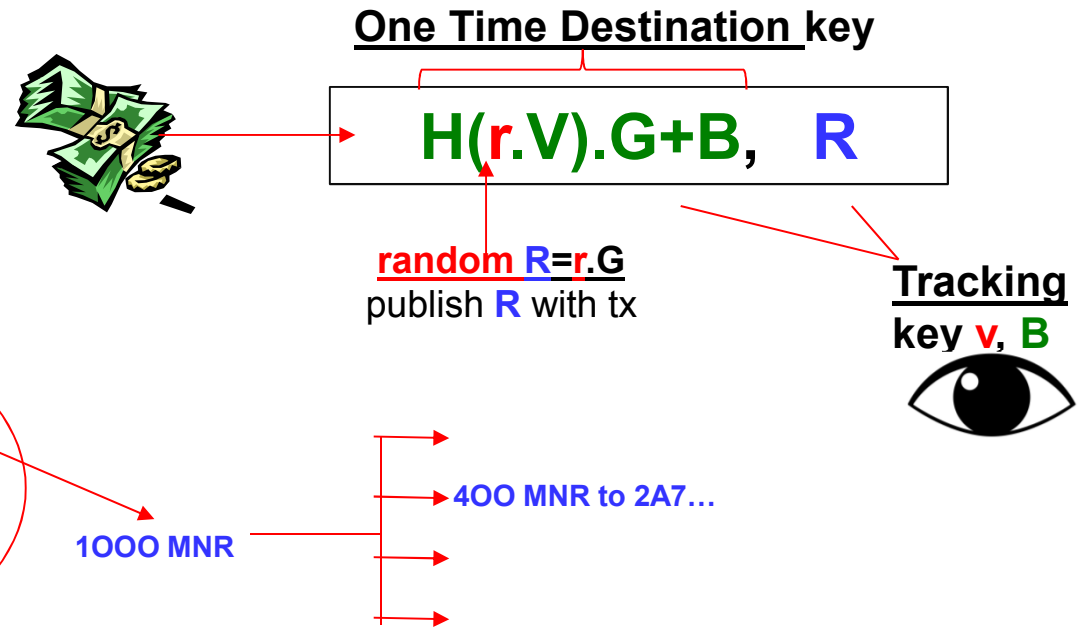
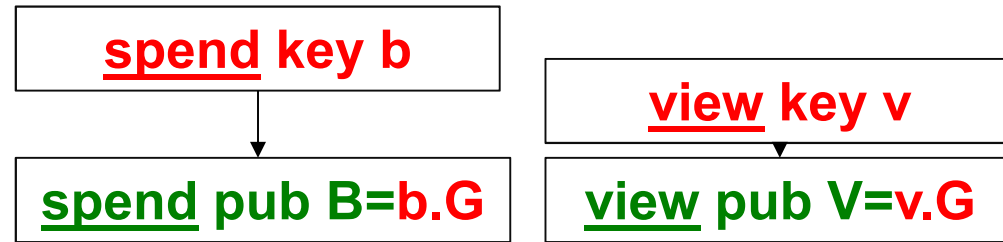
## Better Stealth Address used in Monero

- Recipient/B has **Private User Key** =  $b, v$
- Proxy has **Tracking Key** =  $v, b.G$  (removes anonymity).
- Receiver **Public User key** =  $b.G, v.G$ .

\*fixed  $a$  was replaced by random  $r$

- Let  $S = v.(r.G) = r.(v.G)$ . Sender random  $r$ , publishes  $R = r.G$  with this tx.
- Proxy and Receiver can compute  $v.(r.G)$  for every tx done by any A.
- Sender/A can do  $r.(v.G)$ .
- A sends bitcoins to  $E = b.G + H(S).G$ .
- Proxy does not know  $e$ .
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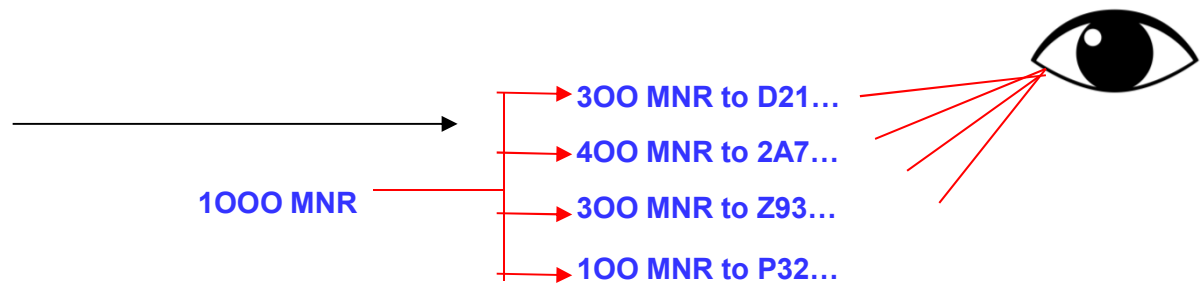
# Sending Monero



**Money from several attributions to PKs: the sender must know the ECDL for ALL these inputs**

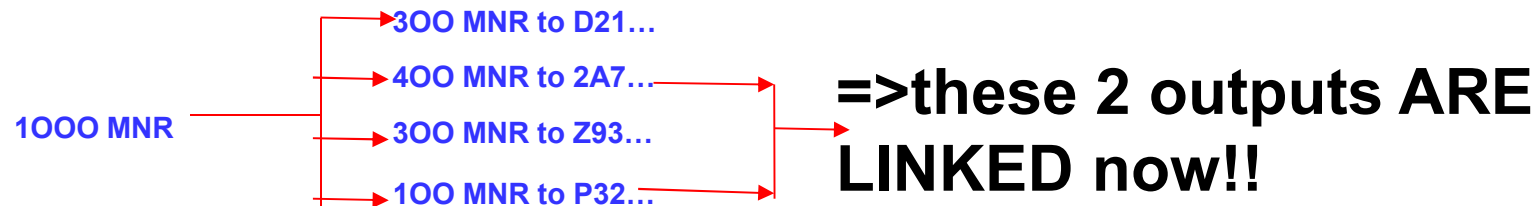
# Privacy – Good?

At this moment:   
NO WAY to know which  
outputs are “change”  
and which are Recipient  
addresses



Pb3.

# Spending reveals information and compromises privacy



## Not Perfect

Paper by Monero labs:

Adam Mackenzie, Surae Noether and Monero Core Team:

“Improving Obfuscation in the CryptoNote Protocol”, Jan’15

<https://lab.getmonero.org/pubs/MRL-0004.pdf>



Citations:

“CryptoNote is very traceable”

[...]

“users **can receive** CryptoNote-based cryptocurrencies with no concern for their privacy, they **cannot necessarily spend** those currencies without releasing some information about their past transactions”

Bitcoin and  
Z.Cash ALSO have  
this problem